

Following Paper ID and Roll No. to be filled in your Answer Book.

PAPER ID : 21109

Roll
No.

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BCA. Examination 2018-2019

(Even Semester)

MATHEMATICS II

Time : Three Hours]

[Maximum Marks : 60

Note :- Attempt all questions.

SECTION – A

1. Attempt all parts of the following : $8 \times 1 = 8$

- Write the set $A = \{ 1, 2, 3, 4, 5, 6, 7, 8 \}$ in the set-builder form.
- If $A = \{ 1, 2, 3 \}$ find $P(A)$
- If a set A has m elements how many relations are there from A to A .
- If the function $f : \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(x) = x^2$, find $f^{-1}(4)$.
- Draw the Hasse diagram for the set of factors of 17 for relation divides.

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- (f) Define poset.
 (g) Find the generator of the cyclic group $G = \{1, 2, 3, 4, 5, 6, \dots\} \times_7$.
 (h) Define integral domain.

SECTION – B

2. Attempt any two parts of the following : $2 \times 6 = 12$

- (a) If A, B and C are sets then prove that

$$A \times (B \cap C) = (A \times B) \cap (A \times C)$$

- (b) Prove that the intersection of two equivalence relations on a set is an equivalence relation on the set.

- (c) Prove that every finite lattice is bounded.

- (d) Show that the set $G = \{1, -1, i, -i\}$ consisting of four fourth roots of unity form an Abelian multiplicative group.

SECTION – C

Note :- Attempt all questions.

3. Attempt any two parts : $2 \times 5 = 10$

- (a) Define following with example:

- (i) Union and intersection of sets
 (ii) Disjoint and intersecting sets
 (b) For any sets A and B prove that :

$$P(A \cap B) = P(A) \cap P(B)$$

- (c) In a group of 65 people 40 like cricket, 10 like cricket and tennis both. How many like tennis only and not cricket? How many like tennis?

4. Attempt any two parts : $2 \times 5 = 10$

- (a) Define relation and explain types of relation.
 (b) Let $X = \{1, 2, 3, 4, 5, 6, 7\}$ and $R = \{(x, y) : x - y \text{ is divisible by } 3\}$ Show that R is an equivalence relation.

- (c) Show that the function f and g both of which are form $N \times N$ to N given by $f(x, y) = x + y$ and $g(x, y) = xy$ are onto but not one one.

5. Attempt any two parts : $2 \times 5 = 10$

- (a) Let $S = \{1, 2, 3\}$ and $A = P(S)$. Draw the Hasse diagram of the poset A with the partial order \subseteq (set inclusion).

- (b) Define bounded lattice and prove that every finite lattice is bounded.

(c) If (L, \wedge, \vee) is complemented distributive lattice then the complement of $a \in L$ is unique.

6. Attempt any two parts : $2 \times 5 = 10$

(a) The necessary and sufficient condition for a non empty subset H of a group $(G, 0)$ to be a subgroup is :

$$a \in H, b \in H \Rightarrow aob^{-1} \in H$$

Where b^{-1} is the inverse of b in G .

(b) Define normal subgroup homomorphism isomorphism.

(c) Prove that every field is an integral domain.
